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# DETERMINATION OF THE NONUNIFORMITY OF VENTILATION BY THE HELIUM MIXING TIME IN THE LUNG - SPIROGRAPH SYSTEM

L. A. Sidorenko

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Dependence of the helium mixing time in the lung-spirograph system of factors influencing its value was analyzed. In the case of uniform ventilation of the lungs graphs were plotted by means of which the "ideal" mixing time was determined. It is suggested that nonuniformity of lung ventilation be judged by the amount by which the mixing time obtained during investigation of the patient's respiration exceeds the "ideal" time found for the same patient from the graph.

KEY WORDS: ventilation of the lungs; helium method; residual lung volume.

The helium method is usually used to determine the residual lung volume. In the course of this investigation data are obtained on the time during which almost uniform mixing of helium takes place in the lung-spirograph system. Attempts are often made to judge the nonuniformity of the lung ventilation by the mixing time without allowing for how it depends on other factors: the longer the mixing time, the greater the nonuniformity of ventilation. However, the mixing time depends not only on the nonuniformity of lung ventilation, but also on indices such as the minute alveolar ventilation, the functional reserve capacity, the volume of the spirograph and initial helium concentration in it, and also on the experimental conditions. The problem thus arises of allowing for the dependence of the helium mixing time in the system on the factors listed above, so that the nonuniformity of alveolar ventilation can be estimated on the basis of this parameter.

The mixing time which the patient should have if his lungs were uniformly ventilated may be called the "ideal" mixing time. Clearly, the greater the nonuniformity of the patient's pulmonary ventilation, the more the mixing time will exceed the "ideal" value found for the same patient, other conditions being the same.

An equation was obtained for determining the "ideal" mixing time  $t$ :

$$t = \left( V_1 V_2 \ln \frac{c_0 u \Delta t}{\Delta c V_1} \right) : [u (V_1 + V_2)], \quad (1)$$

where  $V_1$  is the volume of the spirograph (the bell and dead space of the instrument) before the beginning of the test;  $c_0$  the initial fractional helium concentration in the spirograph;  $V_2$  the functional residual capacity (FRC) of the patient's lungs determined during the investigation;  $u$  the minute alveolar ventilation (MAV);  $\Delta t$  and  $\Delta c$  parameters characterizing the conditions for stopping the investigation.

The time of stopping the investigation can be chosen in different ways by different investigators for this gives different interpretations of the degree of uniformity of mixing. In the general sense the conditions of stopping the investigation can be defined as follows: The investigation is stopped when changes in the helium concentration in the spirograph decrease to a certain small value  $\Delta c$  at time intervals  $\Delta t$  chosen for the observation. Since the aim of the investigation is to compare results obtained in practice with those calculated theoretically, it is important that during theoretical calculation the values of  $\Delta t$  and  $\Delta c$  be chosen to be the same as the conditions of stopping the investigation during experimental determination of the mixing time.

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Department of Functional Diagnosis of the Respiratory Organs, Central Hospital, No. 4 Main Administrative Board, Ministry of Health of the RSFSR, Moscow. (Presented by Academician V. N. Chernigovskii.) Translated from *Byulleten' Éksperimental'noi Biologii i Meditsiny*, Vol. 84, No. 11, pp. 631-632, November, 1977.

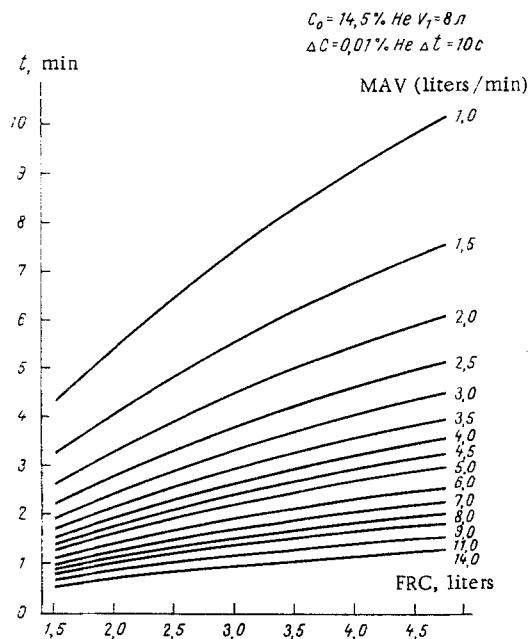


Fig. 1. Determination of "ideal" helium mixing time in the lung-spirograph system. The "ideal" mixing time (ordinate) is found from the value of the functional residual capacity (abscissa) and minute alveolar ventilation (the vertical column of numbers on the right). The parameters for which these graphs were plotted are indicated in the top right-hand corner.

Equation (1) was obtained as follows. Changes in the helium concentration in the spirograph after connection to the patient system can be represented by the following differential equation:

$$V_1 dc_1 = -uc_1 dt + uc_2 dt,$$

where  $c_1$  is the helium concentration in the spirograph;  $c_2$  the same in the lungs;  $dc_1$  the change in the helium concentration in the spirograph during time  $dt$ ;  $uc_2 dt$  the quantity of helium entering the spirograph;  $uc_1 dt$  the quantity of helium leaving the spirograph during time  $dt$ .

Considering that  $c_1 V_1 + c_2 V_2 = c_0 V_1$ , we obtain

$$\frac{dc_1}{dt} = -\left(\frac{u}{V_1} + \frac{u}{V_2}\right)c_1 + \frac{u}{V_2}c_0. \quad (2)$$

Equation (2) can be written in the simplified form

$$\frac{dc_1}{dt} = ac_1 + b, \quad (3)$$

where  $a = \frac{-u(V_1 + V_2)}{V_1 V_2}$  and  $b = \frac{uc_0}{V_2}$ . Substituting in Eq. (3) the variables  $y = ac_1 + b$ , we obtain the differen-

tial equation  $dy/y = a dt$ , which is easily solved. Its solution has the form  $y = k \exp(at)$ . When  $t=0$   $k = uc_0/V_1$  considering the above arguments, we obtain

$$y = -\frac{uc_0}{V_1} \exp\left(-u \frac{V_1 + V_2}{V_1 V_2} t\right).$$

Reverting to the original variable, we obtain a relationship between the helium concentration in the spirograph  $c_1$  and time and the other variables:

$$c_1 = \frac{c_0 V_1}{V_1 + V_2} + \frac{c_0 V_2}{V_1 + V_2} \exp\left(-u \frac{V_1 + V_2}{V_1 V_2} t\right).$$

Considering that the investigation is stopped when the change in the helium concentration in the spirograph during time  $\Delta t$  falls to  $\Delta c$ , it is easy to obtain the Eq. (1) for calculating the "ideal" gas mixing time in the lung-spirograph system.

Repeated calculations of the "ideal" mixing time by Eq. (1) in everyday practice would be a difficult task. Graphs simplifying this process were accordingly plotted. The dependence of the "ideal" time on the value of

FRC for different values of MAV are shown in Fig. 1, for Eq. (1) reduces to the dependence of  $t$  on these two indices. Graphs were plotted from the numerical data obtained by computer using the simplest program for calculating  $t$  by Eq. (1) for different values of  $V_2$  and  $u$ . The remaining parameters in this case were given values corresponding to those obtained experimentally. The volume of the spiograph  $V_1$  and also the initial helium concentration in it  $c_0$  are almost constant under the comparatively uniform conditions of the investigation and they can be taken as known. FRC ( $V_2$ ) is determined for each patient in the course of the investigation. MAV ( $u$ ) is found from the spiographic data. For its determination it is also essential to know the anatomical dead space (ADS), and this can be determined by additional experimental investigations or, if the apparatus required for determination of ADS is not available, the known norms can be used [2, 3]. The values of  $\Delta t$  and  $\Delta c$ , together with the remaining initial data are indicated on Fig. 1. Others more acceptable for other investigators can also be chosen for them. If the initial data differ from those for which the graphs were plotted in this paper, new graphs can be drawn to determine the "ideal" mixing time in accordance with Eq. (1).

Reports of the detection of disturbances of ventilation on the basis of the helium method have been published [1, 4-7]. However, strict, scientifically based "norms" of an index such as the mixing time were not given in these papers. The results of the present investigation enable a "norm" of the helium mixing time, namely the "ideal" mixing time, to be found for each patient and, depending on by how much the true mixing time exceeds the "ideal" time, the nonuniformity of pulmonary ventilation can be judged. The reason for this excess is disturbances of ventilation connected with pathological changes in the respiratory apparatus such as disturbances of bronchial patency, emphysema, compensatory changes in the blood flow, and so on.

Hence, as a result of these calculations and constructions, it was possible to draw valid conclusions regarding the presence or absence of nonuniformity of pulmonary ventilation from the helium mixing time in the lung-spiograph system, so that the mixing time itself acquires definite interest in connection with the comprehensive investigation of external respiration.

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